

Title: APPARATUS AND METHOD USING CONTINUOUS-WAVE
RADIATION FOR DETECTING AND LOCATING TARGETS
HIDDEN BEHIND A SURFACE

SPECIFICATION

CROSS REFERENCE TO RELATED APPLICATIONS

This application claims the benefit of provisional Application No. 60/413,757 filed September 27, 2002, and provisional Application No. 60/474,962 filed June 3, 2003, both incorporated herein by reference.

BACKGROUND OF THE INVENTION

This invention is concerned with the detection and location of targets hidden behind a surface, such as a surface of the earth, using continuous-wave radiation.

Although the detailed description of the invention
5 refers to measurement of reflected electromagnetic radiation at microwave wavelengths, the principles of the invention are applicable to other types of continuous-wave systems, such as those using sound waves (e.g., sonar).

Various means and methods have been developed for
10 detection and location of buried metallic and non-metallic objects which rely on the reflectivity of the objects at radar (microwave) wavelengths. These means and methods

include devices which attempt to image the objects through beam scanning and determine distance (range) by timing differences between transmitted and reflected pulses (i.e., ground-penetrating radars) as well as devices which attempt
5 to utilize expected differences between background (earth) reflectivity and the reflectivity of the buried object. Both methods are subject to significant difficulties in their ability to locate buried objects (especially non-metallic objects) due to several factors. These include:

10 (a) presence of other buried materials in surrounding soil (rocks, tree roots, etc.) whose reflectivities are comparable to that of the target object;

(b) rough or uneven terrain surface which produces widely-varying background reflected signals;

15 (c) for continuous-wave devices, constructive and destructive interference between transmitted and reflected waves;

(d) interference between multi-path reflected signals;
and

20 (e) interference between the fundamental frequency and harmonics in the reflected wave.

Although pulsed devices which rely on timing are less subject to interference problems than continuous-wave

devices, continuous-wave devices are inherently less complex, require less power, and may be made more easily portable.

5 BRIEF DESCRIPTION OF THE INVENTION

The following description relates to a continuous-wave device comprising a transmitter and two or more receivers designed to detect and locate buried metallic and non-metallic objects by measurement of reflected microwave radiation, and discloses the means and methods used to
10 overcome or diminish some of the difficulties described above.

The invention will be described with reference to two embodiments which are designed to detect targets beneath
15 the surface of the earth, but it will become apparent in later portions of the description that the invention is useful in detecting targets hidden behind wall surfaces, for example.

Both embodiments of the invention use a transmitter
20 that transmits a beam of continuous-wave radiation and a pair of receivers of such radiation. Predetermined spatial relationships (geometry) of the transmitter and the receivers are provided such that the transmitter is farther

from the surface than the receivers and such that a quadrature phase relationship exists for reflected radiation at the receivers. In one embodiment, a quadrature relationship also exists for direct radiation
5 that reaches the receivers from the transmitter.

Although not so restricted, in both embodiments the transmitter and the receivers are mounted on an elongated hand-held rod, with the receivers adjacent to an end of the rod and the transmitter farther from the end of the rod
10 than the receivers. For microwave applications of the invention, directional antennas are used at the transmitter and each of the receivers. In one embodiment, the axis of each beam pattern is along the length of the rod. In another embodiment, parallel axes of the receiver beam
15 patterns are inclined with respect to the length of the rod, and the axis of the transmitter beam pattern is also inclined with respect to the length of the rod, but at a different angle of inclination than that for the receivers.

20 BRIEF DESCRIPTION OF THE DRAWINGS

The invention will be further described in conjunction with the accompanying drawings, which illustrate preferred (best mode) embodiments, and wherein:

Fig. 1 is a view showing a first embodiment of the invention in use;

Fig. 2 is a perspective view of the first embodiment;

Fig. 3 is a fragmentary perspective view showing a
5 portion of the first embodiment;

Fig. 4 is a fragmentary perspective view showing another portion of the first embodiment;

Fig. 5 is a plan view of an antenna that can be used in the invention;

10 Fig. 6 is a graphical view showing the results of an actual test of the first embodiment;

Fig. 7 is another graphical view showing test results of the first embodiment;

Fig. 8 is a diagram showing spatial relationships
15 employed in the first embodiment;

Fig. 9 is a view showing a second embodiment of the invention in use;

Fig. 10 is a fragmentary perspective view of the second embodiment;

20 Fig. 11 is a fragmentary elevation view showing a portion of the second embodiment;

Fig. 12 is a perspective view of the second embodiment;

Fig. 13 is diagram showing spatial relationships employed in the second embodiment;

Fig. 14 is another diagram showing spatial relationships employed in the second embodiment; and

5 Figs. 15A and 15B constitute a block diagram showing a circuit that can be used in the second embodiment.

DETAILED DESCRIPTION OF THE INVENTION

First Embodiment

10 Figs. 1-5 show apparatus 10 employed in the first embodiment. In this apparatus, there are three antennas, namely, a transmitter antenna XMTR and two receiver antennas RCV1 and RCV2. In the later description, the receiver antenna RCV2 referred to as the "top antenna" is
15 actually closer to the ground than the "bottom antenna" RCV1 in the use of the apparatus. All three antennas are mounted on a rod 12, such as a 1-inch square fiberglass tube. Basswood blocks 14 are used to attach the antennas to the tube.

20 The two receiver antennas are mounted on opposite sides of the rod 12, and in use the top antenna RCV2 is 0.6 inch closer to the ground than the bottom antenna RCV1. The transmitter antenna XMTR is mounted on the same side of

the rod as the top antenna RCV2 and is at equal distances from the receiver antennas. For example, the transmitter antenna may be ten inches from the receiver antennas. This distance is not critical, but should be the same for both receiver antennas.

In the apparatus shown, each antenna is a directional log periodic antenna having the gain of a Yagi but in a smaller space. See Fig. 5. The antenna elements 16 and 18 are mounted on opposite sides of a PC board 20. The elements on one side of the board are tied to the elements on the opposite side of the board, which are fed with the center conductor of a coaxial cable 22.

As shown in Fig. 2, the rod is angulated and has a handle 24 at one end that is held by an operator when the apparatus is in use as shown in Fig. 1. Mounted on the rod adjacent to the handle is an electronics unit 26 that includes a source of continuous microwave energy, a battery power supply, one or more readout devices (e.g., visual and/or audible) and various controls (e.g., background null and gain adjust). Typical circuitry for use in the invention will be described later in connection with the second embodiment.

In the use of the apparatus, as shown in Fig. 1, a beam of radiation is transmitted into the ground toward a hidden target and radiation reflected from the target is received by the receivers and produces an output.

5 Continuous-Wave Transmitter/Receiver Design

Consideration of factors (a) through (e) above leads to a number of constraints in the design of a continuous-wave detector. Factors (a) and (b) lead to a requirement that the transmitter be situated high enough above the
10 terrain surface that, for a reasonably restricted transmitter beamwidth, the transmitter beam will illuminate an area of the ground that is large compared to the size of the non-target irregularities (rocks, etc.) and terrain roughness scale. The same considerations apply to the
15 height requirement for the receiving antenna(s), subject to the two additional requirements that the receiving antenna(s) must be as close as possible to the ground for maximum sensitivity to the reflected signal from the target, and as far as possible from the transmitter to
20 reduce the direct signal.

Factor (c) above suggests that a pair of receiving antennas separated by some appropriate fraction of a wavelength might be used to insure that both receivers can

never simultaneously be located at an interference null, while (d) and (e) impact the receiver antenna's beamwidth pattern and tuning characteristics, respectively.

Analysis of wave pathlengths and phases indicates that the transmitter antenna must lie above the pair of receiver antennas for the reduction of interference effects.

Fig. 8 shows spatial relationships of the transmitter and the receivers of the first embodiment, and more particularly shows path lengths and phase differences, as follows:

$$\begin{aligned}
 &\text{DIRECT PATHS:} && \text{RCU1: } S1 = a \\
 & && \text{RCU2: } S2 = a + b \\
 &\text{REFLECTED PATHS:} && \text{RCU1: } S1' = Rx + R1 \\
 & && \text{RCU2: } S2' = Rx + R2 \\
 &\text{with: } && Rx = \text{SQR}(x^2 + (a + b + z)^2) \\
 & && R1 = \text{SQR}(x^2 + (b + z)^2) \\
 & && R2 = \text{SQR}(x^2 + z^2) \\
 &\text{DIRECT PHASES:} && \text{RCU1: } Ph1 = 360 a/L + Ph0 \\
 & && \text{RCU2: } Ph2 = 360 (a + b)/L + Ph0 \\
 &\text{with: } && L = \text{wavelength and } Ph0 = \text{constant} \\
 &\text{REFLECTED PHASES:} && \text{RCU1: } Ph1' = 360 S1'/L + Ph0 \\
 & && \text{RCU2: } Ph2' = 360 S2'/L + Ph0 \\
 &\text{PHASE DIFFERENCES:} && \text{RCU1: } d(Ph1) = Ph1' - Ph1 \\
 & && && d(Ph1) = 360 (S1' - a)/L \\
 & && \text{RCU2: } d(Ph2) = Ph2' - Ph2 \\
 & && && d(Ph2) = 360 (S2' - a - b)/L \\
 &\text{TOTAL PHASE DIFFERENCE (RCU1 AND RCU2 REFLECTED SIGNALS):} && \\
 & && d(Ph1) - d(Ph2) = 360 (S1' - S2' + b)/L \\
 &\text{At } x = 0: && S1' = (a + b + z) + (b + z) \\
 & && S2' = (a + b + z) + z \\
 &\text{and: } && d(Ph1) - d(Ph2) = 360 (2b)/L
 \end{aligned}$$

The reflected signals at RCU1 and RCU2 are in quadrature (90 degrees out of phase) when $d(Ph1) - d(Ph2) = 90$, or when:

$$b = L/8$$

In accordance with the invention, the receiving antennas are separated by a distance $b=L/8$ to fix the phase difference between the two receiver antennas at 90°

5 (quadrature) when the antennas are directly above the target. This provides a means of determining the true amplitude of the continuous-wave radiation reflected from the target independent of interference effects. In keeping with the constraints discussed previously, for $b \ll z$, the
10 amplitudes of the reflected signals at RCV1 and RCV2 will be nearly identical, and with 90 degrees phase difference between their addition to the direct signals at RCV1 and at RCV2, which for $b \ll a$ are also nearly identical. Hence, if the direct signals at RCV1 and RCV2 are denoted by A_1 and
15 A_2 , with the reflected signals at RCV1 and RCV2 by A_1' and A_2' , the corresponding total signals T_1 and T_2 may be written:

$$T_1 = A_1 + A_1' \cos(\Phi) \quad \text{and} \quad T_2 = A_2 + A_2' \cos(\Phi + 90) = A_2 + A_2' \sin(\Phi)$$

20

If the direct signals A_1 and A_2 are measured before a target is present and subtracted from outputs T_1 and T_2 ,

then the average reflected signal amplitude A' (which is nearly equal to A_1' and A_2') can be found from:

$$A' = \text{SQR}((T_1 - A_1)^2 + (T_2 - A_2)^2) \sim A_1' \sim A_2' \text{ since } (\sin(\Phi))^2 + (\cos(\Phi))^2 = 1$$

5

Thus the amplitude A' is independent of phase angle Φ (hence without interference effects) when the device is directly above the target ($x=0$). In the following section, it will be shown that A' should be a monotonic function of target distance (z) below the lower receiver antenna RCV2 for horizontal distances small compared to vertical distance ($x \ll z$).

Transmitted and Reflected Signal Strengths

15 The amplitude A' described above is a function of the transmitter power and beam pattern, distance and angle from transmitter to the target, target size, shape and microwave reflectivity, and the distance and angle from the target to the receiving antennas. The following analysis considers
 20 the strength of the transmitted signal at the target, the reflection by the target, and the reflected signal at the receiving antennas. For simplicity, a cylindrical target of radius R_p is assumed with reflectivity Q . The transmitted

signal strength is assumed to fall off as $1/r$, and the antenna pattern for transmitter and receiver is that of a log periodic Yagi with measured cosine 12 angular falloff. Since the length of the cylindrical target illuminated

5 increases with distance in the antenna beam pattern, the strength of the reflected signal will fall off more slowly than $1/r$, and an arbitrary $(1/r)^n$ is assumed for the reflected signal. In the following, the transmitter signal at 1 meter along the vertical axis is denoted A_x .

10 Transmitted signal strength at target:

$$A_t = A_x * ((\cos(\text{Alpha}))^{12}) / R_x \quad \text{where } \tan(\text{Alpha}) = x / (a+b+z)$$

Direct signal strengths at receiver:

$$A_1 = A_x / a \quad \text{and} \quad A_2 = A_x / (a+b)$$

Reflected signal strength at receiver:

$$15 \quad \begin{aligned} A_1' &= Q * A_t * ((\cos(\text{Beta}_1))^{12}) * (R_p / R_1)^n & \text{where } \tan(\text{Beta}_1) &= x / (b+z) \\ A_2' &= Q * A_t * ((\cos(\text{Beta}_2))^{12}) * (R_p / R_2)^n & \text{where } \tan(\text{Beta}_2) &= x / z \end{aligned}$$

A device based on the described design was fabricated and tested. In the test device, the parameters were: wave freq= 2.452897 Ghz ($L = 12.22$ cm.), $a = 21.6$ cm., $b = 1.528$ cm. ($L/8$), and the exponent n was determined to be 0.5.

20 Test results shown in Fig. 6 were obtained for an unburied PVC pipe in air with $R_p = 2.54$ cm. The dashed curve is a normalized theoretical fit from equations set forth earlier.

Discussion of Results

As shown in the data plot in Fig. 6, the combination of the two receiver outputs to obtain total reflected signal amplitude results in a signal which agrees very well with the theoretical prediction. The average deviation of the combined outputs in this plot is approximately 12.5 millivolts. This small deviation is due to combined effects of reflections over the illuminated target length, small differences in the amplitude of the direct and reflected signals at the two receiving antennas, reflections off of nearby objects, and possible interference effects of wave harmonics. By contrast, the interference effects at the two receiver antennas cause deviations as large as +/- 160 millivolts. Thus the 1/8 wavelength offset between the two receiving antennas to obtain quadrature in the two receiver phases provides a means of determining reflected signal amplitude through elimination of the large deviations caused by interference between the direct signal from the transmitter and the reflected signals. Fig. 7 illustrates that the quadrature output greatly reduces the interference pattern variations seen in either receiver output.

The substantial reduction or elimination of interference effects also allows the possibility of using two or more pairs of quadrature receiving antennas, collinear and spaced some distance apart, to determine target depth. By measuring the true reflected signal amplitude at each pair, the theoretical curve of signal strength vs. target distance may be used to determine target distance independent of absolute signal strength. Signal strength may then be used to determine combined reflectivity and target area, which may be helpful in the determination of target characteristics such as composition (metallic or non-metallic, etc.), size and possibly shape.

Applications

- 15 The device described in the previous sections, a combination of a continuous-wave transmitter and two or more pairs of quadrature receiving antennas has a wide range of possible application, including but not limited to:
- 20 (a) detection and location of underground metallic and non-metallic pipes, cables, conduits and utility lines
- (b) detection and location of buried metallic and non-metallic munitions, including mines

(c) detection and location of underground anomalies such as tunnels, shafts or graves.

Tests of the device in an urban environment also indicate that the transmitted and reflected beams are
5 capable of penetrating building walls constructed of wood, sheetrock, stone or brick, and that the reflections produced by anomalies within or behind the walls may be used to locate such anomalies. Related applications include:

10 (a) detection and location of beams, studs, electrical conduit and gas or water pipes within building walls

(b) detection and location of moving objects, including human or animal bodies, behind building walls.

Second Embodiment

15 In the above-described first embodiment of the invention, quadrature of the two receiver phases for reflected radiation eliminates the large deviations caused by interference between the direct signal from the transmitter and the two reflected signals. Additional
20 improvement in performance may be obtained by choice of a geometry in which the transmitter antenna is shifted to the side of the receiver antennas, with the receiver antennas placed so that both the direct wave from the transmitter

and the reflected wave from a target below the receiver antennas are 90 degrees out of phase at the two receiver antennas (direct and reflected wave quadrature). In addition, the re-positioning of the receiver antennas away
5 from the center of the transmitter antenna beam greatly reduces the direct signal strength at both receiver antennas. A further benefit of this design is that the reflected signal from the ground surface is not directly below the receiver antennas, and the transmitter antenna
10 beam may be tilted toward the receiver antennas so that the center of the transmitter beam illuminates a point at a desired depth below the ground surface.

A simple embodiment of the design discussed above comprises the transmitter antenna and the upper of the pair
15 of receiver antennas mounted at opposite ends of a portion of a rigid rod or pole which is inclined at an angle (theta) from the vertical, with the second (lower) receiver antenna suspended below the rod or pole by a rigid strut in such a position that it is $1/4$ wavelength closer to the
20 ground surface than the upper receiver antenna and is also $1/4$ wavelength closer to the transmitter antenna than the upper receiver antenna.

The second embodiment of apparatus 28 of the invention using this design is shown in Figs. 9-12, in which the rod 30 is a 3/4-inch aluminum tube ("main beam"). 1-inch square fiberglass tubing mounting posts 32 (struts) support the transmitter antenna XMTR and receiver antennas RCV1 and RCV2. The transmitter circuit is designated XC. The mounting posts are pinned to the aluminum with 1/4-inch fiberglass tubing and glued in place. Each of the antennas is a directional log periodic type, such as that shown in Fig. 5 described earlier and is enclosed in an ABS plastic box 34. Each receiver antenna has a true power detector at the base of the antenna on the same circuit board. This detector gives a DC voltage output proportional to the detected RF power at the antenna. The transmitter antenna has a short coax cable to the transmitter. The circuitry will be described later.

As shown in Fig. 9, the rod 30 has a handle 36 intermediate its length which is held by an operator when the apparatus is in use. An electronics unit 38 of the type referred to earlier is mounted on the rod between the transmitter and the handle. A battery power supply 40 is mounted on the rod adjacent to the opposite end of the rod

and includes batteries that form a counter-weight for the apparatus.

The geometry (spatial relationships) of such a design is illustrated in Figs. 13 and 14, with theta, the angle from vertical, set to 45 degrees. This choice of angle was made for comfort of use and balance of the device in the user's hands, and is not otherwise prescribed. The receiver antennas RCV1 and RCV2 are disposed in parallel (vertically in Fig. 14). In general, the exact dimensions of the device required for both direct and reflected wave quadrature may be calculated for an arbitrary angle theta and transmitter wavelength L according to the following relationships:

For chosen angle theta and chosen overall distance S1 between transmitter antenna and upper receiver antenna, the lower receiver antenna will be supported at a vertical distance D2 below the inclined rod from a point at a distance k along the rod from the transmitter antenna, with k and D2 calculated from:

$$\begin{aligned} k &= S1 * \text{SQR}(1 - .5 * L * ((1 + \cos(\theta)) / (1 - (\cos(\theta))^2)) / S1) \\ D2 &= L / 4 + (S1 - k) * \cos(\theta) \end{aligned}$$

The vertical displacement h of the transmitter antenna above the lower receiver antenna is given by:

$$h = S1 * \cos(\theta) + L/4$$

and the horizontal distance dx between the two receiver antennas is given by:

$$dx = (S1 - k) * \sin(\theta)$$

- 5 The angle of tilt of the transmitter antenna from vertical (phi) required for the center of the transmitter beam to cross the vertical mid-line between the two receiver antennas at a distance d below the lower receiver antenna is:

$$10 \quad \phi = \arctan((S1 * \sin(\theta) - dx/2) / (h + d))$$

Fig. 14 shows path lengths and phase differences in the second embodiment, as follows:

DIRECT PATHS: RCU1: S1
RCU2: S2 = S1 - L/4

15 REFLECTED PATHS: RCU1: S1' = Rx + R1
RCU2: S2' = Rx + R2
with: Rx = $\sqrt{(x^2 - x)^2 + (h + z)^2}$
R1 = $\sqrt{(x + dx)^2 + (z + L/4)^2}$
R2 = $\sqrt{x^2 + z^2}$

DIRECT PHASES: RCU1: Ph1 = $360 * S1 / L + \text{Ph0}$
RCU2: Ph2 = $360 * S2 / L + \text{Ph0}$
with: L = wavelength and Ph0 = constant

DIRECT PHASE DIFFERENCE: d(Phi) = Ph1 - Ph2 = 90 (QUADRATURE)

REFLECTED PHASES: RCU1: Ph1' = $360 * S1' / L + \text{Ph0}$
RCU2: Ph2' = $360 * S2' / L + \text{Ph0}$

REFLECTED PHASE DIFFERENCE: d(Phi') = Ph1' - Ph2' = $360 * (R1 - R2) / L$
d(Phi') = $360 * (\sqrt{(x + dx)^2 + (z + L/4)^2} - \sqrt{x^2 + z^2}) / L$

For $z \gg dx$, at $x = -dx/2$:
d(Phi') = 90 (QUADRATURE)

Thus in this preferred design, both the direct signals and the reflected signals at RCV1 and RCV2 are in quadrature (90 degrees out of phase) when the target is along a vertical line mid-way between the two receiver
5 antennas.

As shown, the transmitter antenna is tilted 15 degrees from the vertical, corresponding to the center of the transmitter beam crossing the vertical mid-line of the two receiver antennas at a point 15 inches below the RCV2
10 antenna for $S_1=12.00$ inches.

Selection of the various parameters (θ , S_1 , d_1 , and Z_f) specifying the instrument geometry involves trade-off between instrument size, balance and ease of handling, and expected target burial depth. The choices of parameters and
15 factors involved in their selection are discussed below.

Transmitter-Receiver Distance (S_1) and Angle from

Vertical (θ)

Since both receiver antennas RCV1 and RCV2 are always vertical, selection of S_1 for any particular value of θ
20 determines both the horizontal displacement between the transmitter antenna and the receiver antennas and the height of the transmitter above the ground. As previously discussed, the transmitter height above the ground should

be sufficient for the transmitted beam to illuminate a spot on the ground whose area is much larger than that of irregularities on the ground or at shallow depths below it. This produces an average ground background which remains

5 relatively constant, since it averages over many irregularities. However, the transmitter antenna should be far enough away from the feet of the user that the user's feet do not produce reflections in the process of walking normally while carrying the instrument. Likewise, the

10 combination of S_1 and θ should position the two receiver antennas RCV1 and RCV2 close enough to the buried target to receive a strong reflected signal, but high enough above the ground surface to average over surface irregularities reflections. A natural design scheme places the balance

15 point at the user's hand, with the batteries providing a rear counter-weight for the weight of the antennas and electronics. A practical limit of 52 inches was chosen for overall length, and experimenting with various combinations of S_1 and θ for the required battery and instrument weights

20 led to a selection of $S_1=12$ inches and $\theta=45^\circ$ as the optimum configuration for all requirements.

Distance of RCVI Antenna Below Main Support Beam (d_1)

This distance depends entirely on the physical dimensions of the rectangular box enclosing the receiver antenna RCV1 and associated rf detector. At $\theta = 45^\circ$, the minimum possible distance between the main support beam and the center of the receiver antenna RCV1 was $d_1 = 3.5$ in. with d_2 calculated to be 8.42 in.

Focus Depth of Transmitter Beam (Z_t)

The transmitter and receiver antennas beam patterns are identical, sharply focused around the forward direction with power (or sensitivity) dropping to 50% at $\pm 19^\circ$ about the forward axis. Since the receiver antennas are always vertical in operation, the maximum reflected wave signal strength at the receiver antennas will be obtained when the target is along a vertical line mid-way between the two receiver antennas and is illuminated at the center of the transmitter antenna beam. Thus, for an expected average target burial depth, the transmitter antenna angle from vertical θ may be adjusted to have the antenna beam center cross the vertical line between RCV1 and RCV2 at the expected target distance. In the case of mines, the expected burial depth is shallow (3 to 12 inches), whereas in the case of utility lines and pipes, burial may be

expected to be deeper (12 to 36 inches). For test purposes, a value of $Z_e = 15$ inches was chosen, resulting in $\theta = 15^\circ$ and $d_{\text{MT}} = 4.95$ inches, with $L_1 = 13.82$ inches and $L_2 = 8.56$ inches.

5

Instrument Set-up and Operation

As shown in Figs. 15A and 15B, the instrument output consists of an analog voltage (0-10 v.d.c.) which drives both a voltage controlled oscillator (VCO) and a voltmeter. The output voltage V_{out} is developed from the two receiver
 10 r.f. outputs from RCV1 (V1) and RCV2 (V2) through a series of amplifiers and summing circuits, as described below:

(A) Both receiver antenna (RCV1 and RCV2) outputs are measured in power detectors whose output voltages A_1 and A_2 are inputs to difference amplifiers with x10 gain. The
 15 other inputs to the difference amplifiers are voltages from trim pots C_1 and C_2 . The outputs from the two difference amplifiers are thus $10(A_1 - C_1)$ and $10(A_2 - C_2)$.

(B) These outputs go to two variable gain amplifiers with adjustable gain f , whose outputs are $10f(A_1 - C_1)$ and $10f$
 20 $(A_2 - C_2)$.

(C) These outputs are squared, then summed together and the square root of the resultant sum obtained. This voltage

$$V_0 = \text{SQR} [(10f(A_1 - C_1))^2 + (10f(A_2 - C_2))^2]$$

which is equivalent to $V_0 = 10f \text{SQR} [(A_1 - C_1)^2 + (A_2 - C_2)^2]$

(D) The output V_0 and an offset voltage C_0 from a trim pot are inputs to a difference amplifier whose output is $V_0 - C_0$.

5 (E) The output $V_0 - C_0$ is then input to a variable gain amplifier whose gain g is set to: $g = 10/(10 - C_0)$ which sets the output to the meter and VCO so that their full range is scaled (0-10v) as V_0 varies from C_0 to ZC_0 .

10 The instrument is set up for operation in the following steps:

1. Calibration for Direct signals at RCV1 and RCV2

With the antennas pointed upward at the sky,

(a) the meter input is switched to the output
15 developed in step (B) for RCV1, which is $10f(A_1 - C_1)$ and the voltage C_1 is adjusted in the variable pot until the meter reading is 0 (i.e., $C_1 = A_1$). This pot setting is held for RCV1.

(b) meter input is switched to output for RCV2, which
20 is $10f(A_2 - C_2)$ Pot voltage C_2 is adjusted until meter reading is 0 ($C_2 = A_2$) and pot setting is held for RCV2.

(c) Meter input is switched to the output from step (D), which is $V_0 - C_0$.

2. Neutralization of Earth Background

With the device held in normal operating position,
with antennas pointed toward the ground in a location

5 assumed to have no nearby buried targets,

(a) set pot adjusting voltage C_0 to mid-range

(b) adjust variable gain f until meter reading is zero

(c) start research for buried objects, adjusting pot
controlling C_0 as squelch control to compensate for changes
10 in earth background with terrain changes (gravel, bare
earth, grass, etc.)

While preferred embodiments of the invention have been
shown and described, it will be apparent that changes can
be made without departing from the principles and spirit of
15 the invention, the scope of which is defined in the
accompanying claims.